

# EXPANDING AND CONDENSING LOGARITHMS



**Product Property:**  $\log_b AC = \log_b A + \log_b C$

**Quotient Property:**  $\log_b \frac{A}{C} = \log_b A - \log_b C$

**Power Property:**  $\log_b A^k = k \cdot \log_b A$

PROPERTIES OF LOGARITHMS



**Product Property:**  $\log_b AC = \log_b A + \log_b C$

PROPERTIES OF LOGARITHMS

A decorative graphic consisting of several parallel white lines of varying lengths, slanted upwards from left to right, located in the bottom right corner of the slide.

**EX. EXPRESS AS A SUM OF LOGARITHMS.**

$$\mathbf{1) \log_a MN} = \log_a M + \log_a N$$

$$\mathbf{2) \log_b AT} = \log_b A + \log_b T$$

$$\mathbf{3) \log MATH}$$

$$= \log M + \log A + \log T + \log H$$

**EX. EXPRESS AS A SINGLE LOGARITHM**

$$\begin{aligned} 4) \log_5 19 + \log_5 3 &= \log_5 (19 \cdot 3) \\ &= \log_5 57 \end{aligned}$$

$$\begin{aligned} 5) \log C + \log A + \log B + \log I + \log N \\ &= \log CABIN \end{aligned}$$

► Expanding the Logarithm (Write as a sum of logarithms):

$$\log_3(81 \cdot 9) =$$

$$\log_2(8 \cdot 4) =$$

$$\log(5x) =$$

**ON YOUR OWN**

► Expanding the Logarithm (Write as a sum of logarithms):

$$\log_3(81 \cdot 9) =$$

$$\log_3 81 + \log_3 9$$

$$\log_2(8 \cdot 4) =$$

$$\log_2 8 + \log_2 4$$

$$\log(5x) =$$

$$\log 5 + \log x$$

**ON YOUR OWN**

**EX. EXPRESS AS A SUM OF LOGARITHMS, THEN SIMPLIFY.**

**6)  $\log_2 (4 \cdot 16)$  =  $\log_2 4 + \log_2 16$**

$2^? = 4$

$2^? = 16$

$= 2 + 4$

$= 6$



**Quotient Property**  $\log_b \frac{A}{C} = \log_b A - \log_b C$

PROPERTIES OF LOGARITHMS



$$8) \quad \log_a \frac{M}{N} = \log_a M - \log_a N$$

$$9) \quad \log_a \frac{1}{4} = \log_a 1 - \log_a 4$$

**EX. EXPAND (EXPRESS AS A DIFFERENCE)**

► Expanding the Logarithm (Write as a difference of logs):

$$\log_3\left(\frac{1}{27}\right) =$$

$$\log_2\left(\frac{4}{64}\right) =$$

$$\log_5\left(\frac{3}{4}\right) =$$

**ON YOUR OWN**

► Expanding the Logarithm (Write as a difference of logs):

$$\log_3\left(\frac{1}{27}\right) = \log_3 1 - \log_3 27$$

$$\log_2\left(\frac{4}{64}\right) = \log_2 4 - \log_2 64$$

$$\log_5\left(\frac{3}{4}\right) = \log_5 3 - \log_5 4$$

**ON YOUR OWN**

**Power Property:**  $\log_b A^k = k \cdot \log_b A$

PROPERTIES OF LOGARITHMS



**EX. EXPRESS AS A PRODUCT.**

$$11) \log_b 9^{-5} = -5 \cdot \log_b 9$$

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$$12) \log_a \sqrt[4]{5} = \log_a 5^{\frac{1}{4}}$$
$$= \frac{1}{4} \cdot \log_a 5$$

► Expanding the Logarithms:

$$\log_3 (81)^5 =$$

$$\log_3 \sqrt{27} =$$

$$\log_2 (32)^3 =$$

$$\log_2 \sqrt{32} =$$

**ON YOUR OWN**

► Expanding the Logarithms:

$$\log_3(81)^5 =$$

$$5 \log_3 81$$

$$\log_3 \sqrt{27} =$$

$$\log_3 27^{1/2} = \frac{1}{2} \log_3 27$$

$$\log_2(32)^3 =$$

$$3 \log_2 32$$

$$\log_2 \sqrt{32} =$$

$$\log_2 32^{1/2} = \frac{1}{2} \log_2 32$$

**ON YOUR OWN**



# EX. 14 EXPAND $\log 5x^3y$

$$= \log 5 + \log x^3 + \log y$$

$$= \log 5 + 3 \log x + \log y$$

QUO

PRO

POW

EX. 15 EXPAN  $\log_{10} \frac{4\pi}{\sqrt{23}}$

$$= \log_{10} 4\pi - \log_a \sqrt{23}$$

$$= \log_{10} 4 + \log_{10} \pi - \log_a \sqrt{23}$$

$$= \log_{10} 4 + \log_{10} \pi - \log_a 23^{\frac{1}{2}}$$

$$= \log_{10} 4 + \log_{10} \pi - \frac{1}{2} \log_a 23$$

QUO

PRO

POW

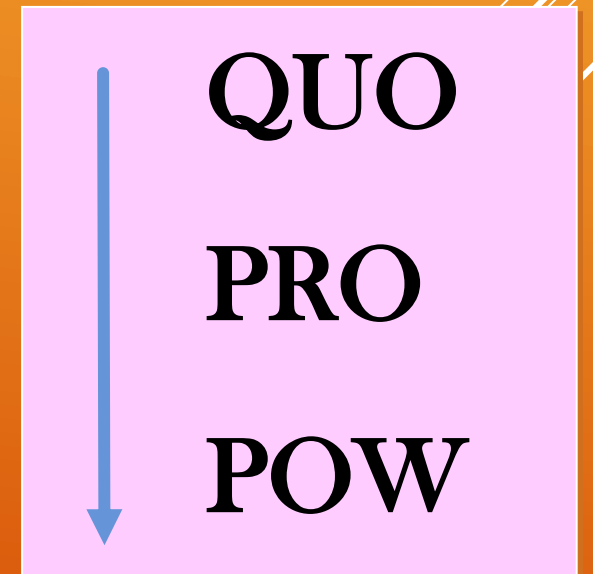
► Expanding the Logarithms:

$$\log\left(\frac{xy}{z}\right) =$$

$$\log\left(\frac{x^3 y}{z}\right) =$$

$$\log x^2 y =$$

ON YOUR OWN



► Expanding the Logarithms:

$$\log\left(\frac{xy}{z}\right) =$$

$$\log\left(\frac{x^3y}{z}\right) =$$

$$\log x^2y =$$

$$\log xy - \log z$$
$$\log x + \log y - \log z$$

$$\log x^3y - \log z$$
$$\log x^3 + \log y - \log z$$
$$3 \log x + \log y - \log z$$

$$\log x^2 + \log y$$
$$2 \log x + \log y$$

ON YOUR OWN

**Complete Practice Lesson 4.6 (1– 4, 11 – 28).**

**CLASSWORK**



## EX. CONDENSE.

$$\begin{aligned} 16) \quad 3 \log x + \frac{1}{2} \log y &= \log x^3 + \log y^{\frac{1}{2}} \\ &= \log x^3 + \log \sqrt{y} \\ &= \log x^3 \sqrt{y} \end{aligned}$$

$$17) \quad 2 \log(x + 2) - \log x = \log(x + 2)^2 - \log x$$

$$= \log \frac{(x + 2)^2}{x}$$

## EX 18 CONDENSE

$$\log_a x^5 - \log_a y + \frac{1}{4} \log_a z$$

$$= \log_a x^5 - \log_a y + \log_a z^{\frac{1}{4}}$$

$$= \log_a x^5 - \log_a y + \log_a \sqrt[4]{z}$$

$$= \log_a \frac{x^5}{y} + \log_a \sqrt[4]{z}$$

$$= \log_a \frac{x^5 \sqrt[4]{z}}{y}$$

- Express all products as exponents
- Change the fractional exponent to a radical sign.
- Simplify the subtraction.
- Simplify the addition.

# PROPERTIES OF LOGARITHMS

$$\log_a 1 = 0 \quad \text{because } a^0 = 1$$

$$\log_a a = 1 \quad \text{because } a^1 = a$$

$$\log_a a^x = x \quad a^{\log_a x} = x$$

$$\text{If } \log_a x = \log_a y \quad \text{then } x = y$$

$$\log_a (uv) = \log_a u + \log_a v \quad \text{Product Property}$$

$$\log_a \frac{u}{v} = \log_a u - \log_a v \quad \text{Quotient Property}$$

$$\log_a u^n = n \log_a u \quad \text{Power Property}$$

$$\log_a x = \frac{\log_{10} x}{\log_{10} a} \quad \text{Change-of-Base}$$



**Warning!! Be careful!!**

$$\log(x + y) \neq \log x + \log y$$

$$\log(x - y) \neq \frac{\log x}{\log y}$$

$$\log(x + y) \neq \log x \cdot \log y$$